TABLE OF CONTENTS

1.0 INTRODUCTION	2
2.0 DESIGN CHARTS	3
2.1 WT BRACE	3
2.1.1 WT Brace Under Compression	3
2.1.1.1 WT Brace Compression – Non X-Brace Case	3
2.1.1.2 WT Brace Compression –X-Brace Case	32
2.1.2 WT Brace Under Tension	62
2.2 DOUBLE ANGLE BRACE	73
2.2.1 Double Angle Brace Under Compression	73
2.2.1.1 Vertical Double Angle Brace	73
2.2.1.1.1 Double Angle Brace Compression – Non X-Brace Case	75
2.2.1.1.1.1 Equal Angle Back-to-Back	76
2.2.1.1.1.2 Unequal Angle Long Leg Back-to-Back	98
2.2.1.1.2 Double Angle Brace Compression –X-Brace Case	111
2.2.1.1.2.1 Equal Angle Back-to-Back	112
2.2.1.1.2.2 Unequal Angle Long Leg Back-to-Back	132
2.2.1.2 Horizontal Double Angle Brace	145
2.2.1.2.1 Double Angle Brace Compression – Non X-Brace Case	146
2.2.1.2.1.1 Equal Angle Back-to-Back	147
2.2.1.2.2 Double Angle Brace Compression – X-Brace Case	167
2.2.1.2.2.1 Equal Angle Back-to-Back	168
2.2.2 Double Angle Brace Under Tension	188
2.2.2.1 Vertical Double Angle Brace	188
2.2.2.1.1 Equal Angle Back-to-Back	190
2.2.2.1.2 Unequal Angle Long Leg Back-to-Back	198
2.2.2.2 Horizontal Double Angle Brace	203
2.2.2.2.1 Equal Angle Back-to-Back	204

Dongxiao Wu P. Eng.

1.0 INTRODUCTION

Singly symmetric sections WT and double angle are widely used in steel structure as bracing members. STAAD Pro's code check ratio output of these singly symmetric members are useless due to the following limitations

- 1. Eccentric Moment Not Considered in STAAD for WT and Double Angle Code Check STAAD output code check ratio is based on pure compression/tension case, which is not correct as there is an eccentric moment applied due to brace connection. The correct code check shall consider the combination of axial tension /compression+ flexure, which actually yields a much lower capacity. From the following design charts we can see the brace actual tension/compression resistance under combined tension/compression + flexure can be only 35% of pure tension/compression case.
- 2. Complexities on Applying Eccentric Moment to Brace Member in STAAD for Code Check The eccentricity of brace force varies based on brace type (WT or double angle) and brace location (horizontal or vertical). The eccentric moment also varies in direction based on tension or compression force, which causes the tee stem in tension or compression and different flexural capacity. Considering the different load combinations causing different tension/compression forces in brace, it's impractical to apply eccentric moment manually in STAAD for code check.
- 3. Complexities on Defining Correct Brace Member Local Axis, In-Plane and Out-of-Plane Unsupported Length There are tremendous complexities to get a brace member correctly modeled/defined in STADD model for correct code checking. For example, the double angle X-bracing, engineers shall define correct in-plane and out-of- plane Ly, Lz value, check member's local axis to make sure it's correct in terms of ry, rz corresponding to previous defined Ly, Lz etc.
- 4. Code Checking on Class 4 Member Not Available in STAAD STAAD does not design Class 4 section. Class 4 section is valid for use in steel structure. The engineers have to work around this by defining lower yield strength in STAAD, section by section, to make it pass the code check. This is very time consuming process.

To simplify the code checking of WT and double angle bracing member, design charts and tables are created based on CSA S16-09 for quick member capacity lookup. These design charts and tables eliminate the complexities by sorting the charts and tables in different criteria. By looking up the charts and tables in the desired category, the engineers will get the correct brace design parameters (eccentricity and moment, in-plane and out-of-plane unsupported length, eccentric moment direction) automatically and find the brace tension/compression capacity in seconds.

- For X-bracing, correct in-plane and out-of-plane unsupported length is implemented in terms of brace location (horizontal or vertical) and brace type (WT or double angle)
- Correct eccentric moment is applied in terms of brace location (horizontal or vertical) and brace type (WT or double angle)
- The eccentric moment is applied at right direction in terms of brace location (horizontal or vertical) and brace type (WT or double angle). This will cause the WT or double angle's stem in the correct tension or compression case.
- Class 4 member capacity is available. Class 4 member is designed using the effective area per CSA S16-09 clause 13.3.5 (a)

2011-03-08 Rev 1.5 Page 2 of 211

Dongxiao Wu P. Eng.

2.0 DESIGN CHARTS

2.1 WT BRACE

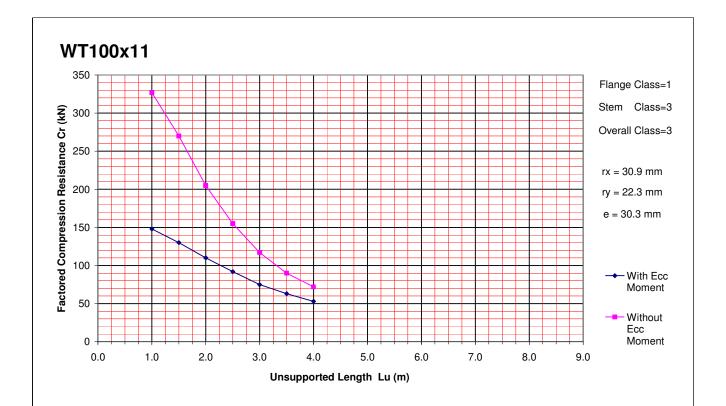
2.1.1 WT Brace Under Compression

2.1.1.1 WT Brace Compression – Non X-Brace Case

Design Basis & Assumption:

- 1. WT compression resistance capacity for two cases, with and without eccentric moment presence are presented.
- 2. The eccentric moment is calculated using gusset plate thickness =10mm. The eccentricity value is shown in each chart.
- 3. The capacity curve stops if next 0.5m increase of unsupported length causes KL/r ratio exceeding 200.
- 4. Assume WT unsupported length Lx = Ly = 1.0L and Kx = Ky = 1.0
- 5. WT brace design yield strength = 50 ksi =345 MPa
- 6. Section class is shown in each chart. For class 4 member, the effective area is used for calculation as per CSA S16-09 clause 13.3.5 (a)
- 7. WT flexural capacity is calculated based on AISC 360-05 section F9
- 8. Assume P-δ (small delta) is not performed in steel frame stability calculation. The U1 factor (CSA S16-09 clause 13.8.4) is calculated and applied for WT strength and stability check as per CSA S16-09 clause 13.8.3

2011-03-08 Rev 1.5 Page 3 of 211

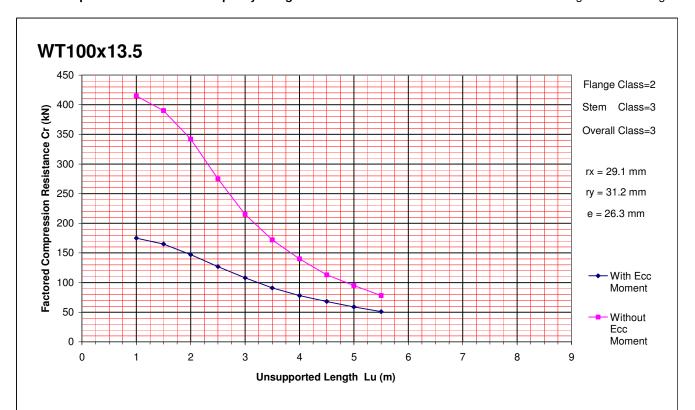


WT100x11

Lu	Cr - ECC	Cr - No ECC
m	kN	kN
1.0	148	327
1.5	130	270
2.0	110	205
2.5	92	155
3.0	75	117
3.5	63	90
4.0	53	72
4.5	0	0
5.0	0	0
5.5	0	0
6.0	0	0
6.5	0	0
7.0	0	0
7.5	0	0
8.0	0	0
8.5	0	0
9.0	0	0

2011-03-08 Rev 1.5 Page 4 of 211





WT100x13.5

Lu	Cr - ECC	Cr - No ECC
m	kN	kN
1.0	175	415
1.5	165	390
2.0	147	342
2.5	127	275
3.0	108	215
3.5	91	172
4.0	78	140
4.5	68	113
5.0	59	95
5.5	51	78
6.0	0	0
6.5	0	0
7.0	0	0
7.5	0	0
8.0	0	0
8.5	0	0
9.0	0	0

2011-03-08 Rev 1.5 Page 5 of 211

2.1.1.2 WT Brace Compression –X-Brace Case

Design Basis & Assumption

1. X-Bracing Out-of-Plane Unsupported Length

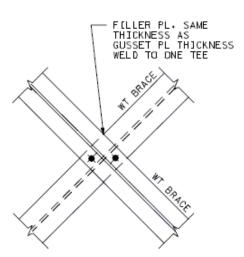
In X-bracing design where two braces are connected at midpoint, some engineers may consider the brace in tension can be counted on to laterally brace the compression strut at midpoint against out-of-plane buckling. Reference is made to AISC Engineering Journal 4th Quarter 1997 "Practical Application of Energy Methods to Structural Stability Problems" by R. Shankar Nair. The out-of-plane stiffness of the intersection point of the braces must be calculated to determine if the tension member can be taken as a brace for the compression member.

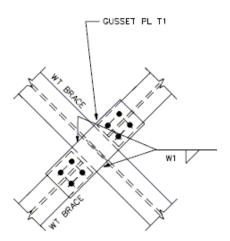
Since it is not practical to do such calculation for every X-bracing and the result may not be positive even the calculation is done, we assume in X-bracing design the out-of-plane unsupported length is full length and the in-plane unsupported length is half length.

WT Brace Intersect Point Connection

WT Vertical Brace

WT Horizontal Brace

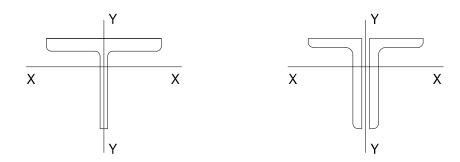




2011-03-08 Rev 1.5 Page 32 of 211



WT and Double Angle Brace Local Axis



For both horizontal and vertical case, used Lx = 1.0L, Ly = 0.5L for all X-bracing compression capacity calculation.

- 2. For all design charts in this section we assume the X-bracing member can take compression force. For Tension Only X-bracing member design please refer to tension capacity charts.
- 3. WT compression resistance capacity for two cases, with and without eccentric moment presence are presented.
- 4. The eccentric moment is calculated using gusset plate thickness =10mm. The eccentricity value is shown in each chart.
- 5. The capacity curve stops if next 0.5m increase of unsupported length causes KL/r ratio exceeding 200.
- 6. Assume WT unsupported length Lx = 1.0L, Ly = 0.5L and Kx = Ky = 1.0
- 7. WT brace design yield strength = 50 ksi =345 MPa
- 8. Section class is shown in each chart. For class 4 member, the effective area is used for calculation as per CSA S16-09 clause 13.3.5 (a)
- 9. WT flexural capacity is calculated based on AISC 360-05 section F9
- 10. Assume P- δ (small delta) is not performed in steel frame stability calculation. The U1 factor (CSA S16-09 clause 13.8.4) is calculated and applied for WT strength and stability check as per CSA S16-09 clause 13.8.3
- 11. For all WT sections, only sections with rx > ry get higher capacity when Lx=1.0L and Ly=0.5L

These sections are

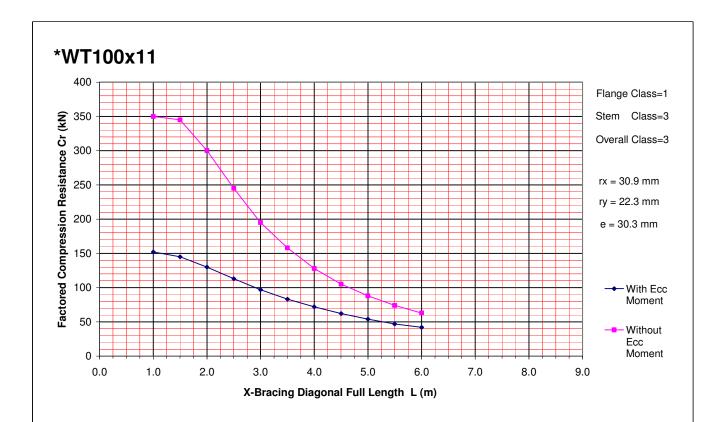
WT100x11

WT125x12.5 WT125x16.5 WT125x19.5 WT125x22.5

WT155x19.5 WT155x22.5 WT155x26

These sections are marked with "*" in the chart

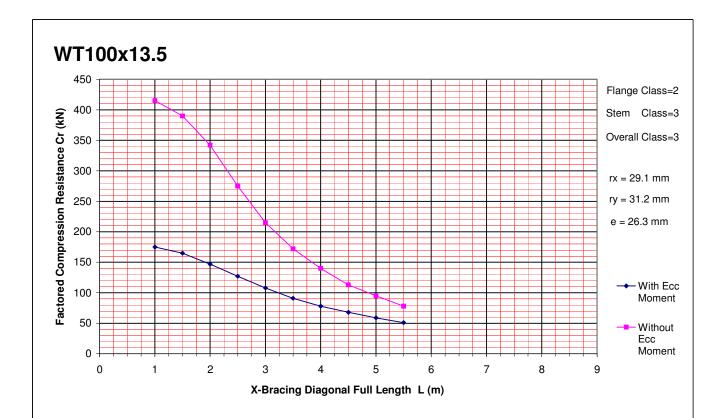
2011-03-08 Rev 1.5 Page 33 of 211



*WT100x11

X-Brace	Cr - ECC	Cr - No ECC
Diagonal Full Length L (m)	kN	kN
1.0	152	350
1.5	145	345
2.0	130	300
2.5	113	245
3.0	97	195
3.5	83	158
4.0	72	128
4.5	62	105
5.0	54	88
5.5	47	74
6.0	42	63
6.5	0	0
7.0	0	0
7.5	0	0
8.0	0	0
8.5	0	0

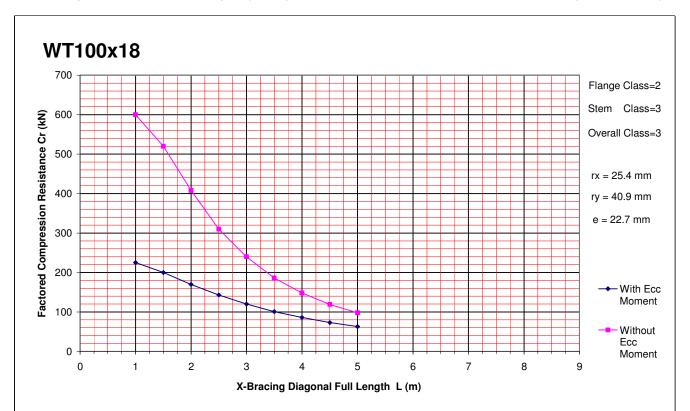
2011-03-08 Rev 1.5 Page 34 of 211



WT100x13.5

X-Brace Diagonal Full	Cr - ECC	Cr - No ECC
Length L (m)	kN	kN
1.0	175	415
1.5	165	390
2.0	147	342
2.5	127	275
3.0	108	215
3.5	91	172
4.0	78	140
4.5	68	113
5.0	59	95
5.5	51	78
6.0	0	0
6.5	0	0
7.0	0	0
7.5	0	0
8.0	0	0
8.5	0	0

2011-03-08 Rev 1.5 Page 35 of 211



WT100x18

X-Brace	Cr - ECC	Cr - No ECC
Diagonal Full Length L (m)	kN	kN
1.0	225	600
1.5	200	520
2.0	170	408
2.5	143	310
3.0	120	240
3.5	101	186
4.0	86	148
4.5	73	119
5.0	63	98
5.5	0	0
6.0	0	0
6.5	0	0
7.0	0	0
7.5	0	0
8.0	0	0
8.5	0	0

2011-03-08 Rev 1.5 Page 37 of 211

Dongxiao Wu P. Eng.

2.1.2 WT Brace Under Tension

Design Basis & Assumption:

- 1. WT <u>member capacity</u> under tension + eccentric moment governs the design. Brace <u>connection capacity</u>, including the effective net area caused by shear lag (CSA S16-09 clause 12.3.3.2), does not govern the design.
- 2. The eccentric moment is calculated using gusset plate thickness =10mm. The eccentricity value is shown in each chart.
- 3. WT maximum unsupported length is calculated as $L_{max} = min(rx, ry) \times 300$ as per CSA S16-09 clause 10.4.2.2
- 4. WT brace design yield strength = 50 ksi =345 MPa
- 5. WT flexural capacity is calculated based on AISC 360-05 section F9, tee stem in compression case.

2011-03-08 Rev 1.5 Page 62 of 211

Dongxiao Wu P. Eng.

T_r – WT factored tension resistance capacity considering eccentric moment, CSA S16-09 clause 13.9

 $T_{1.0}-100\%$ of ($\phi A_g F_y$) CSA S16-09 clause 13.2 (a) (i)

T_{0.5} - 50% of (ϕ A_g F_y), this is normally the value used for connection design for connections without specified design force

L_{max} - Maximum allowed brace unsupported length, CSA S16-09 clause 10.4.2.2

WT100x11

WT Tension Capacity

 $T_r = 126$ kN $L_{max} = 6690$ mm $T_{1.0} = 444$ kN $T_{0.5} = 222$ kN

WT Section Properties

 $r_x = 30.9 \text{ mm}$ $r_y = 22.3 \text{ mm}$ e = 30.3 mm

WT Section Class

FLG= 1 Stem= 3 Overall = 3

WT100x13.5

WT Tension Capacity

 $T_r = 147$ kN $L_{max} = 8730$ mm $T_{1.0} = 528$ kN $T_{0.5} = 264$ kN

WT Section Properties

 $r_x = 29.1 \text{ mm}$ $r_y = 31.2 \text{ mm}$ e = 26.3 mm

WT Section Class

FLG= 2 Stem= 3 Overall = 3

WT100x15.5

WT Tension Capacity

 $T_r = 167 \text{ kN}$ $L_{max} = 8550 \text{ mm}$ $T_{1.0} = 621 \text{ kN}$ $T_{0.5} = 311 \text{ kN}$

WT Section Properties

 $r_x = 28.5 \text{ mm}$ $r_y = 32.0 \text{ mm}$ e = 26.1 mm

WT Section Class

FLG= 1 Stem= 3 Overall = 3

Dongxiao Wu P. Eng.

T_r – WT factored tension resistance capacity considering eccentric moment, CSA S16-09 clause 13.9

 $T_{1.0}$ – 100% of (ϕ A_g F_y) CSA S16-09 clause 13.2 (a) (i)

T_{0.5} - 50% of (ϕ A_g F_y), this is normally the value used for connection design for connections without specified design force

L_{max} - Maximum allowed brace unsupported length, CSA S16-09 clause 10.4.2.2

WT100x18

WT Tension Capacity

$$T_r = 180$$
 kN $L_{max} = 7620$ mm $T_{1.0} = 711$ kN $T_{0.5} = 356$ kN

WT Section Properties

$$r_x = 25.4 \text{ mm}$$
 $r_y = 40.9 \text{ mm}$ $e = 22.7 \text{ mm}$

WT Section Class

WT100x21

WT Tension Capacity

$T_r = 205$ kN $L_{max} = 7770$ mm $T_{1.0} = 826$ kN $T_{0.0}$	$_{0.5} = 413$	kN
---	----------------	----

WT Section Properties

$$r_x = 25.9 \text{ mm}$$
 $r_y = 41.2 \text{ mm}$ $e = 23.8 \text{ mm}$

WT Section Class

WT100x23

WT Tension Capacity

$$T_r =$$
 223 kN $L_{max} =$ **7410** mm $T_{1.0} =$ 910 kN $T_{0.5} =$ 455 kN

WT Section Properties

$$r_x = 24.7 \text{ mm}$$
 $r_y = 51.2 \text{ mm}$ $e = 22.0 \text{ mm}$

WT Section Class

2.2 DOUBLE ANGLE BRACE

2.2.1 Double Angle Brace Under Compression

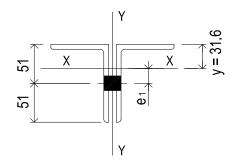
2.2.1.1 Vertical Double Angle Brace

Design Basis & Assumption

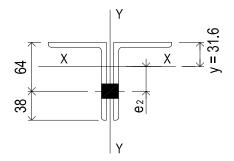
- 1. Assume gusset plate thickness = 10mm → section radius of gyration ry is calculated based on double angle back-to-back with 10mm gap
- 2. Assume the double angle brace is bolt connected and this will create eccentricity between bolt center line (force center line) and section's X-X axis line. The eccentricity is calculated as the maximum of
 - e₁ calculated assuming bolt center line is at center line of angle leg
 - e₂ calculated assuming bolt center line is at AISC recommended gauge line of angle leg

In the following example the eccentricity is calculated as $e = max(e_1, e_2) = 32.4mm$

2L102x76x6.4 LLBB BOLTED VERTICAL BRACE ECCENTRICITY



BOLT AT LEG CENTER LINE e1 = 51 - 31.6 = 19.4 mm



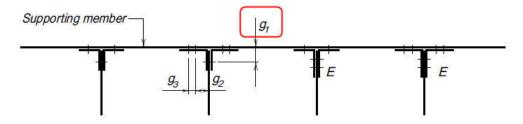
BOLT AT GAUGE LINE e₂ = 64 - 31.6 = 32.4 mm

2011-03-08 Rev 1.5 Page 73 of 211

 The bolt gauge used for double angle connection is based on AISC Manual of Steel Construction 2nd Edition Figure 9-5 on Page 9-13

All-Bolted Double-Angle Connections

Tables 9-2 are design aids for all-bolted double-angle connections. Design strengths are tabulated for supported and supporting member material, as well as angle material with



E indicates that eccentricity must be considered in this leg. Gages g_1 , g_2 , g_3 are usual gages as shown below

				,	Usual	gages	* in ar	ngle le	gs, in.	N .				
Leg	8	7	6	5	4	31/2	3	21/2	2	13/4	11/2	13/8	11/4	1
g_1	41/2	4	31/2	3	21/2	2	13/4	13/8	11/8	1	7/8	7/8	3/4	5/8
g_2 g_3	3 3	2½ 3	21/4 21/2	2 1 ³ / ₄										

Figure 9-5. Eccentricity in double-angle connections.

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- 4. Double angle compression resistance capacity for two cases, with and without eccentric moment presence are presented.
- 5. The capacity curve stops if next 0.5m increase of unsupported length causes KL/r ratio, including modified slenderness ratio considering interconnection bolt at spacing = 1200 mm, exceeding 200.
- 6. Double angle brace design yield strength =300 MPa
- 7. Section class is shown in each chart. For class 4 member, the effective area is used for calculation as per CSA S16-09 clause 13.3.5 (a)
- 8. Double angle flexural capacity is calculated based on AISC 360-05 section F9, stem in compression case.
- Assume double angle brace has interconnecting batten plate and 3/4" dia. bolt at spacing = 1200 mm
 Modified slenderness ratio is used as per AISC 360-05 E6-1 to account for interconnection bolt at spacing = 1200 mm
- 10. Assume P-δ (small delta) is not performed in steel frame stability calculation. The U1 factor (CSA S16-09 clause 13.8.4) is calculated and applied for WT strength and stability check as per CSA S16-09 clause 13.8.3

2011-03-08 Rev 1.5 Page 74 of 211

Dongxiao Wu P. Eng.

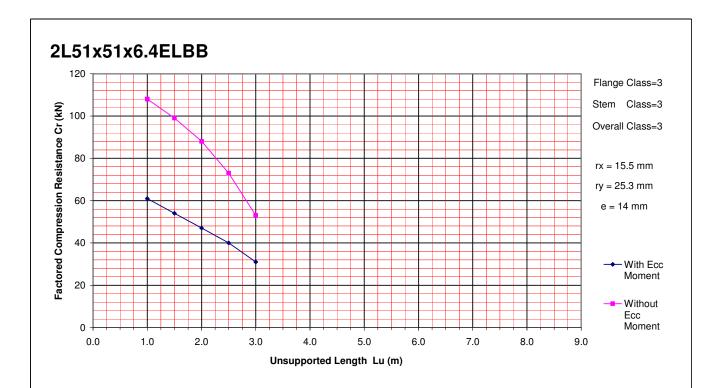
2.2.1.1.1 Double Angle Brace Compression – Non X-Brace Case

Design Basis & Assumption

- 1. All Design Basis & Assumption on Section 2.2.1.1 Vertical Double Angle Brace apply to this section
- 2. Assume double angle unsupported length Lx = Ly = 1.0L and Kx = Ky = 1.0

2011-03-08 Rev 1.5 Page 75 of 211

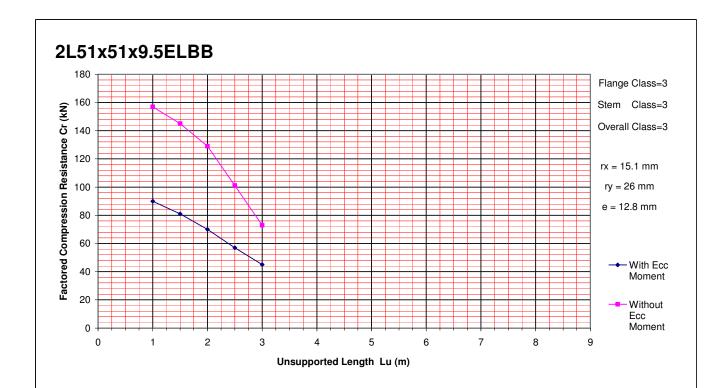
2.2.1.1.1.1 Equal Angle Back-to-Back



2L51x51x6.4ELBB

Lu	Cr - ECC	Cr - No ECC
m	kN	kN
1.0	61	108
1.5	54	99
2.0	47	88
2.5	40	73
3.0	31	53
3.5	0	0
4.0	0	0
4.5	0	0
5.0	0	0
5.5	0	0
6.0	0	0
6.5	0	0
7.0	0	0
7.5	0	0
8.0	0	0
8.5	0	0
9.0	0	0

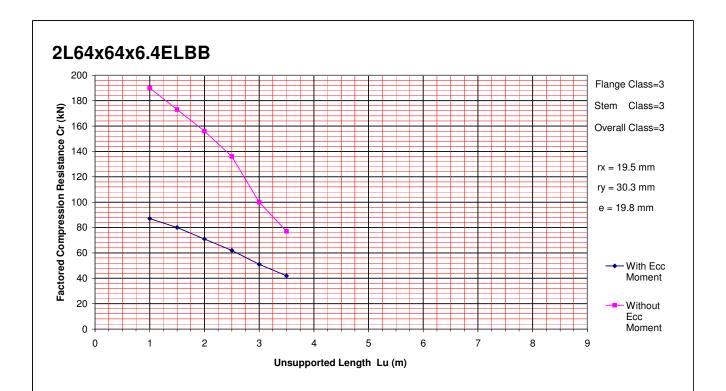
2011-03-08 Rev 1.5 Page 76 of 211



2L51x51x9.5ELBB

Lu	Cr - ECC	Cr - No ECC
m	kN	kN
1.0	90	157
1.5	81	145
2.0	70	129
2.5	57	101
3.0	45	73
3.5	0	0
4.0	0	0
4.5	0	0
5.0	0	0
5.5	0	0
6.0	0	0
6.5	0	0
7.0	0	0
7.5	0	0
8.0	0	0
8.5	0	0
9.0	0	0

2011-03-08 Rev 1.5 Page 77 of 211



2L64x64x6.4ELBB

Lu	Cr - ECC	Cr - No ECC
m	kN	kN
1.0	87	190
1.5	80	173
2.0	71	156
2.5	62	136
3.0	51	100
3.5	42	77
4.0	0	0
4.5	0	0
5.0	0	0
5.5	0	0
6.0	0	0
6.5	0	0
7.0	0	0
7.5	0	0
8.0	0	0
8.5	0	0
9.0	0	0

2011-03-08 Rev 1.5 Page 78 of 211



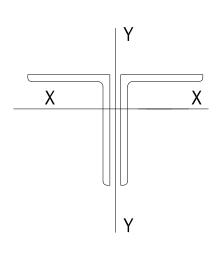
2.2.1.1.2 Double Angle Brace Compression –X-Brace Case

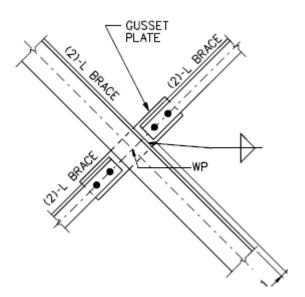
Design Basis & Assumption

- 1. Design charts in this section apply to vertical double angle X-bracing
- 2. All Design Basis & Assumption on Section 2.2.1.1 Vertical Double Angle Brace apply to this section
- 3. For vertical double angle X-bracing, use unsupported length Lx = 0.5L and Ly = 1.0L, Kx = Ky = 1.0

Double Angle Section Local Axis

Vertical Double Angle X-Bracing
Intersect Point Connection

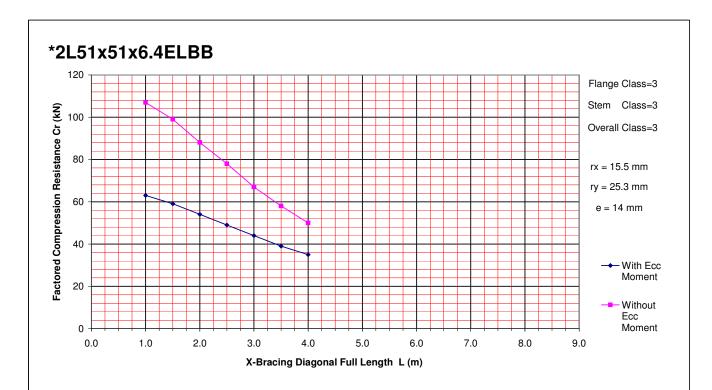




- 4. For all equal leg double angle sections, rx < ry, all sections get higher capacity due to X-bracing's unsupported length Lx = 0.5L and Ly =1.0L
- 5. All sections getting higher capacity due to rx < ry are marked with "*" in the chart

2011-03-08 Rev 1.5 Page 111 of 211

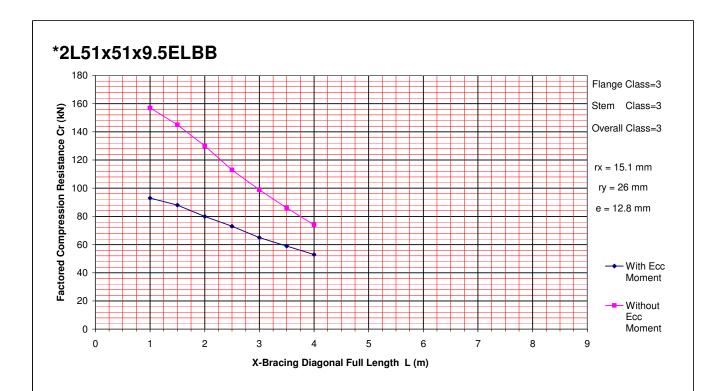
2.2.1.1.2.1 Equal Angle Back-to-Back



*2L51x51x6.4ELBB

X-Brace	Cr - ECC	Cr - No ECC
Diagonal Full L (m)	kN	kN
1.0	63	107
1.5	59	99
2.0	54	88
2.5	49	78
3.0	44	67
3.5	39	58
4.0	35	50
4.5	0	0
5.0	0	0
5.5	0	0
6.0	0	0
6.5	0	0
7.0	0	0
7.5	0	0
8.0	0	0
8.5	0	0
9.0	0	0

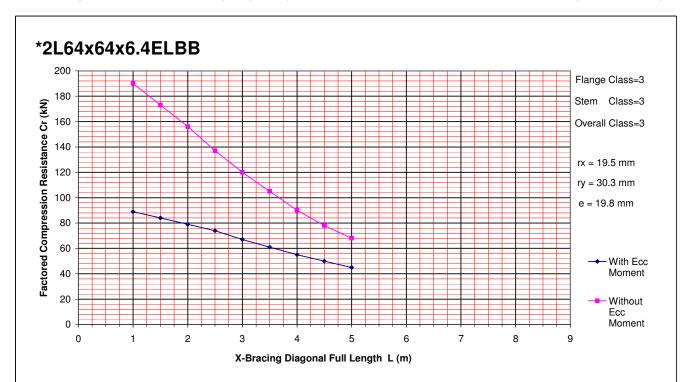
2011-03-08 Rev 1.5 Page 112 of 211



*2L51x51x9.5ELBB

X-Brace	Cr - ECC	Cr - No ECC		
Diagonal Full L (m)	kN	kN		
1.0	93	157		
1.5	88	145		
2.0	80	130		
2.5	73	113		
3.0	65	99		
3.5	59	86		
4.0	53	74		
4.5	0	0		
5.0	0	0		
5.5	0	0		
6.0	0	0		
6.5	0	0		
7.0	0	0		
7.5	0	0		
8.0	0	0		
8.5	0	0		
9.0	0	0		

2011-03-08 Rev 1.5 Page 113 of 211

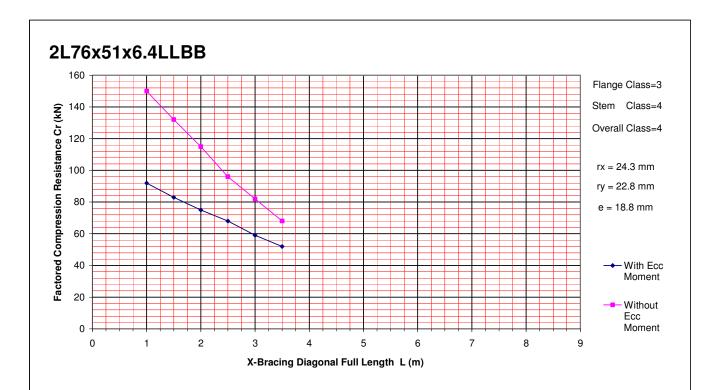


*2L64x64x6.4ELBB

X-Brace	Cr - ECC	Cr - No ECC
Diagonal Full L (m)	kN	kN
1.0	89	190
1.5	84	173
2.0	79	156
2.5	74	137
3.0	67	120
3.5	61	105
4.0	55	90
4.5	50	78
5.0	45	68
5.5	0	0
6.0	0	0
6.5	0	0
7.0	0	0
7.5	0	0
8.0	0	0
8.5	0	0
9.0	0	0

2011-03-08 Rev 1.5 Page 114 of 211

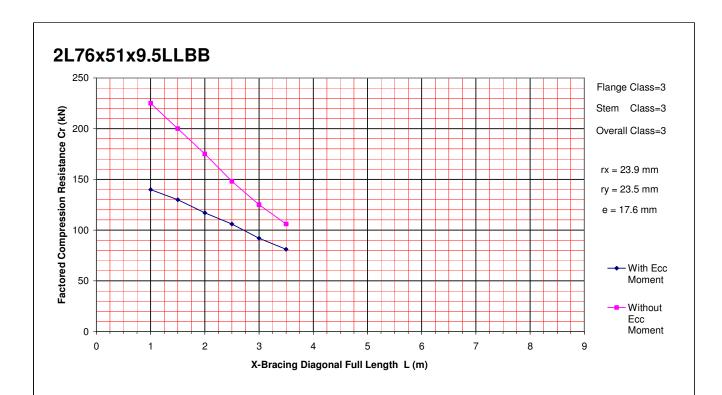
2.2.1.1.2.2 Unequal Angle Long Leg Back-to-Back



2L76x51x6.4LLBB

X-Brace	Cr - ECC	Cr - No ECC			
Diagonal Full L (m)	kN	kN			
1.0	92	150			
1.5	83	132			
2.0	75	115			
2.5	68	96			
3.0	59	82			
3.5	52	68			
4.0	0	0			
4.5	0	0			
5.0	0	0			
5.5	0	0			
6.0	0	0			
6.5	0	0			
7.0	0	0			
7.5	0	0			
8.0	0	0			

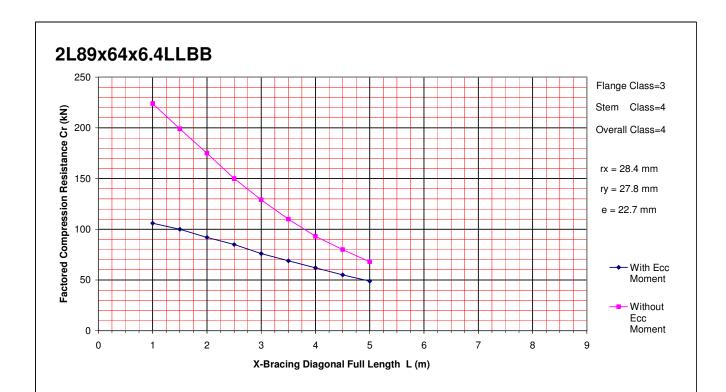
2011-03-08 Rev 1.5 Page 132 of 211



2L76x51x9.5LLBB

X-Brace	Cr - ECC	Cr - No ECC
Diagonal Full L (m)	kN	kN
1.0	140	225
1.5	130	200
2.0	117	175
2.5	106	148
3.0	92	125
3.5	81	106
4.0	0	0
4.5	0	0
5.0	0	0
5.5	0	0
6.0	0	0
6.5	0	0
7.0	0	0
7.5	0	0
8.0	0	0

2011-03-08 Rev 1.5 Page 133 of 211



2L89x64x6.4LLBB

X-Brace	Cr - ECC	Cr - No ECC
Diagonal Full L (m)	kN	kN
1.0	106	224
1.5	100	199
2.0	92	175
2.5	85	150
3.0	76	129
3.5	69	110
4.0	62	93
4.5	55	80
5.0	49	68
5.5	0	0
6.0	0	0
6.5	0	0
7.0	0	0
7.5	0	0
8.0	0	0

2011-03-08 Rev 1.5 Page 134 of 211

Dongxiao Wu P. Eng.

2.2.1.2 Horizontal Double Angle Brace

Design Basis & Assumption

- 1. Double angle section radius of gyration ry is calculated based on double angle back-to-back with 0mm gap
- 2. The eccentric moment is calculated using gusset plate thickness =10mm. The eccentricity value is shown in each chart.
- 3. Double angle compression resistance capacity for two cases, with and without eccentric moment presence are presented.
- 4. The capacity curve stops if next 0.5m increase of unsupported length causes KL/r ratio, including modified slenderness ratio considering interconnection bolt at spacing = 1200 mm, exceeding 200.
- 5. Double angle brace design yield strength =300 MPa
- 6. Section class is shown in each chart. For class 4 member, the effective area is used for calculation as per CSA S16-09 clause 13.3.5 (a)
- 7. Double angle flexural capacity is calculated based on AISC 360-05 section F9, stem in tension case.
- 8. Assume double angle brace has interconnecting 3/4" dia. bolt at spacing = 1200 mm. Modified slenderness ratio as per AISC 360-05 E6-1 is used to account for interconnection bolt at spacing = 1200 mm.
- 9. Assume P-δ (small delta) is not performed in steel frame stability calculation. The U1 factor (CSA S16-09 clause 13.8.4) is calculated and applied for WT strength and stability check as per CSA S16-09 clause 13.8.3

2011-03-08 Rev 1.5 Page 145 of 211

Dongxiao Wu P. Eng.

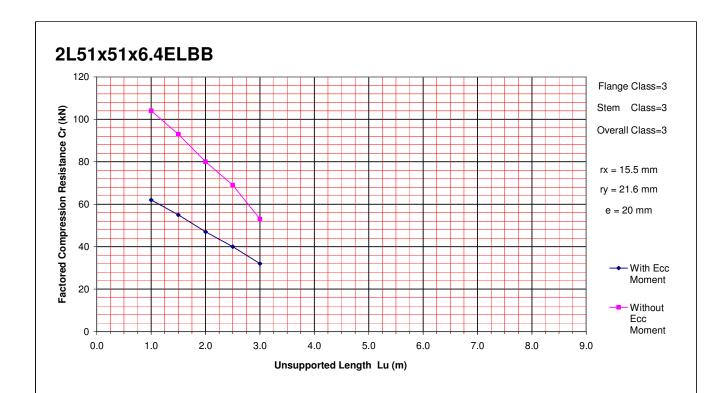
2.2.1.2.1 Double Angle Brace Compression – Non X-Brace Case

Design Basis & Assumption

- 1. All Design Basis & Assumption on Section 2.2.1.2 Horizontal Double Angle Brace apply to this section
- 2. Assume double angle unsupported length Lx = Ly = 1.0L and Kx = Ky = 1.0

2011-03-08 Rev 1.5 Page 146 of 211

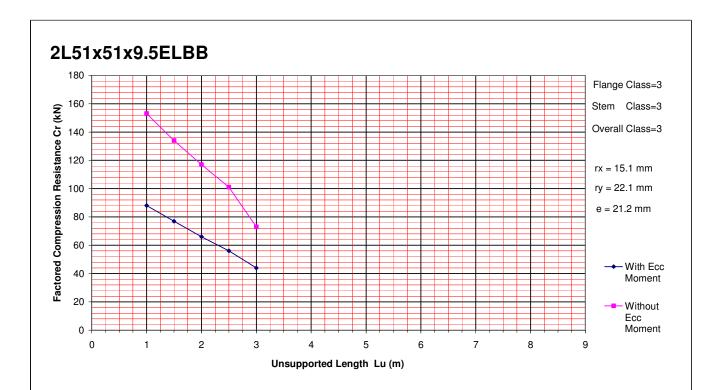
2.2.1.2.1.1 Equal Angle Back-to-Back



2L51x51x6.4ELBB

Lu	Cr - ECC	Cr - No ECC
m	kN	kN
1.0	62	104
1.5	55	93
2.0	47	80
2.5	40	69
3.0	32	53
3.5	0	0
4.0	0	0
4.5	0	0
5.0	0	0
5.5	0	0
6.0	0	0
6.5	0	0
7.0	0	0
7.5	0	0
8.0	0	0

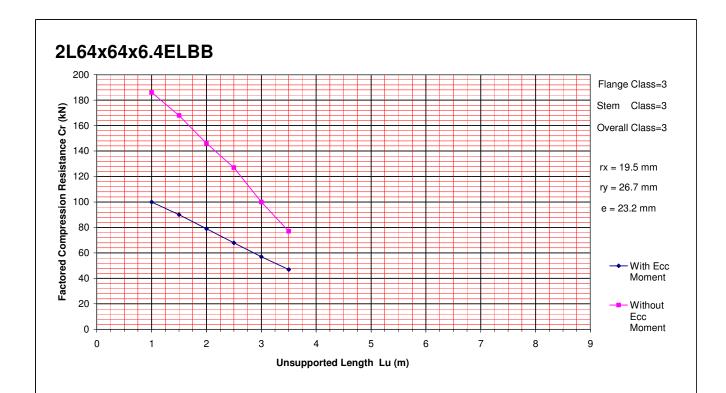
2011-03-08 Rev 1.5 Page 147 of 211



2L51x51x9.5ELBB

Lu	Cr - ECC	Cr - No ECC
m	kN	kN
1.0	88	153
1.5	77	134
2.0	66	117
2.5	56	101
3.0	44	73
3.5	0	0
4.0	0	0
4.5	0	0
5.0	0	0
5.5	0	0
6.0	0	0
6.5	0	0
7.0	0	0
7.5	0	0
8.0	0	0

2011-03-08 Rev 1.5 Page 148 of 211



2L64x64x6.4ELBB

Lu	Cr - ECC	Cr - No ECC
m	kN	kN
1.0	100	186
1.5	90	168
2.0	79	146
2.5	68	127
3.0	57	100
3.5	47	77
4.0	0	0
4.5	0	0
5.0	0	0
5.5	0	0
6.0	0	0
6.5	0	0
7.0	0	0
7.5	0	0
8.0	0	0

2011-03-08 Rev 1.5 Page 149 of 211



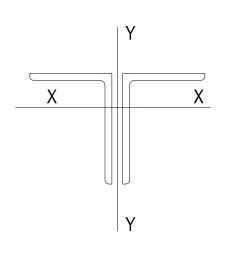
2.2.1.2.2 Double Angle Brace Compression – X-Brace Case

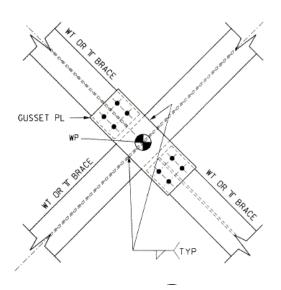
Design Basis & Assumption

- 1. Design charts in this section apply to horizontal double angle X-bracing
- 2. All Design Basis & Assumption on Section 2.2.1.2 Horizontal Double Angle Brace apply to this section
- 3. For horizontal double angle X-bracing, use unsupported length Lx = 1.0L and Ly = 0.5L, Kx = Ky = 1.0

Double Angle Section Local Axis

Horizontal Double Angle X-Bracing Intersect Point Connection

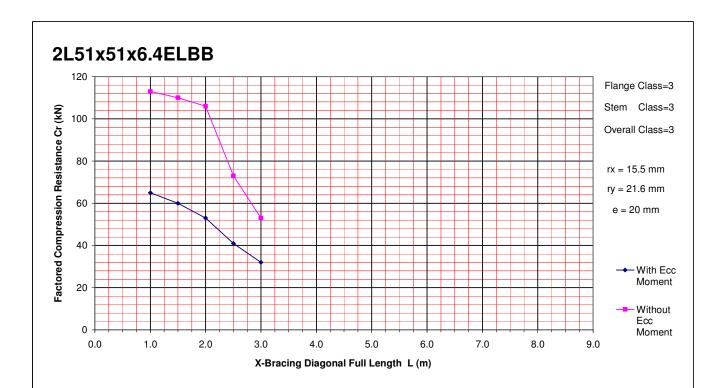




4. For all equal leg double angle sections, rx < ry, none of the equal leg angle section gets higher capacity due to X-bracing's unsupported length Lx = 1.0L and Ly = 0.5L

2011-03-08 Rev 1.5 Page 167 of 211

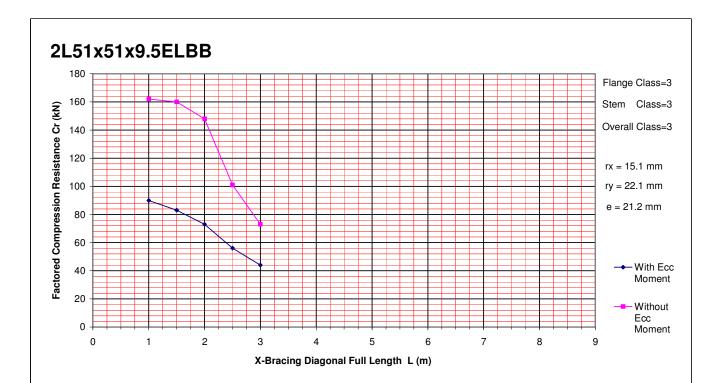
2.2.1.2.2.1 Equal Angle Back-to-Back



2L51x51x6.4ELBB

X-Bracing Diagonal Full	Cr - ECC	Cr - No ECC
Length L (m)	kN	kN
1.0	65	113
1.5	60	110
2.0	53	106
2.5	41	73
3.0	32	53
3.5	0	0
4.0	0	0
4.5	0	0
5.0	0	0
5.5	0	0
6.0	0	0
6.5	0	0
7.0	0	0
7.5	0	0
8.0	0	0
8.5	0	0

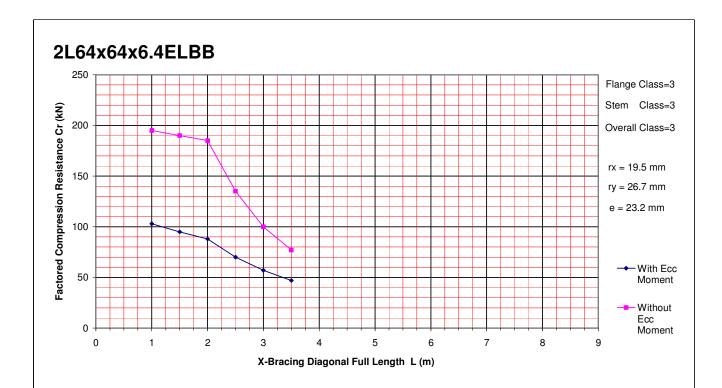
2011-03-08 Rev 1.5 Page 168 of 211



2L51x51x9.5ELBB

X-Bracing	Cr - ECC	Cr - No ECC
Diagonal Full Length L (m)	kN	kN
1.0	90	162
1.5	83	160
2.0	73	148
2.5	56	101
3.0	44	73
3.5	0	0
4.0	0	0
4.5	0	0
5.0	0	0
5.5	0	0
6.0	0	0
6.5	0	0
7.0	0	0
7.5	0	0
8.0	0	0
8.5	0	0

2011-03-08 Rev 1.5 Page 169 of 211



2L64x64x6.4ELBB

X-Bracing	Cr - ECC	Cr - No ECC
Diagonal Full Length L (m)	kN	kN
1.0	103	195
1.5	95	190
2.0	88	185
2.5	70	135
3.0	57	100
3.5	47	77
4.0	0	0
4.5	0	0
5.0	0	0
5.5	0	0
6.0	0	0
6.5	0	0
7.0	0	0
7.5	0	0
8.0	0	0
8.5	0	0

2011-03-08 Rev 1.5 Page 170 of 211

2.2.2 Double Angle Brace Under Tension

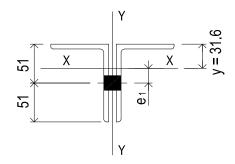
2.2.2.1 Vertical Double Angle Brace

Design Basis & Assumption

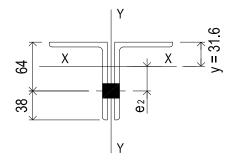
- 1. Assume gusset plate thickness = 10mm → section radius of gyration ry is calculated based on double angle back-to-back with 10mm gap
- 2. Assume the double angle brace is bolt connected and this will create eccentricity between bolt center line (force center line) and section's X-X axis line. The eccentricity is calculated as the maximum of
 - e₁ calculated assuming bolt center line is at center line of angle leg
 - e₂ calculated assuming bolt center line is at AISC recommended gauge line of angle leg

In the following example the eccentricity is calculated as $e = max(e_1, e_2) = 32.4mm$

2L102x76x6.4 LLBB BOLTED VERTICAL BRACE ECCENTRICITY



BOLT AT LEG CENTER LINE e1 = 51 - 31.6 = 19.4 mm



BOLT AT GAUGE LINE e₂ = 64 - 31.6 = 32.4 mm

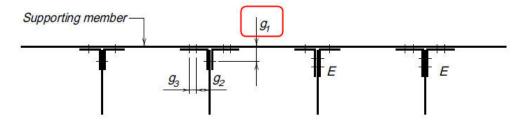
2011-03-08 Rev 1.5 Page 188 of 211

Dongxiao Wu P. Eng.

 The bolt gauge used for double angle connection is based on AISC Manual of Steel Construction 2nd Edition Figure 9-5 on Page 9-13

All-Bolted Double-Angle Connections

Tables 9-2 are design aids for all-bolted double-angle connections. Design strengths are tabulated for supported and supporting member material, as well as angle material with



E indicates that eccentricity must be considered in this leg. Gages g_1 , g_2 , g_3 are usual gages as shown below

					Usual	gages	* in ar	ngle le	gs, in.	ē				
Leg	8	7	6	5	4	31/2	3	21/2	2	13/4	11/2	13/8	11/4	1
g_1	41/2	4	31/2	3	21/2	2	13/4	13/8	11/8	1	7/8	7/8	3/4	5/8
g_2 g_3	3	2½ 3	21/4 21/2	2 1 ³ / ₄										

Figure 9-5. Eccentricity in double-angle connections.

AMERICAN INSTITUTE OF STEEL CONSTRUCTION

- 4. Double angle brace design yield strength =300 MPa
- 5. Section class is shown in each chart. For class 4 member, the effective area is used for calculation as per CSA S16-09 clause 13.3.5 (a)
- 6. Double angle flexural capacity is calculated based on AISC 360-05 section F9, stem in tension case.
- 6. Double angle <u>member capacity</u> under tension + eccentric moment governs the design. Brace <u>connection capacity</u>, including the effective net area caused by shear lag (CSA S16-09 clause 12.3.3.2), does not govern the design.
- 7. Double angle maximum unsupported length is calculated as $L_{max} = min(rx, ry) \times 300$ as per CSA S16-09 clause 10.4.2.2

2011-03-08 Rev 1.5 Page 189 of 211

Dongxiao Wu P. Eng.

2.2.2.1.1 Equal Angle Back-to-Back

Tr - Double angle factored tension resistance capacity considering eccentric moment, CSA S16-09 clause 13.9

 $T_{1.0}$ – 100% of (ϕ A_g F_y) CSA S16-09 clause 13.2 (a) (i)

T_{0.5} - 50% of (ϕ A_q F_v), this is normally the value used for connection design for connections without specified design force

Lmax - Maximum allowed brace unsupported length, CSA S16-09 clause 10.4.2.2

2L51x51x6.4ELBB

Double Angle Tension Capacity

 $T_r = 140$ kN $L_{max} = 4650$ mm $T_{1.0} = 327$ kN $T_{0.5} = 163$ kN

Double Angle Section Properties

 $r_x = 15.5 \text{ mm}$ $r_y = 25.3 \text{ mm}$ e = 14.0 mm

Double Angle Section Class

FLG= 3 Stem= 3 Overall = 3

2L51x51x9.5ELBB

Double Angle Tension Capacity

 $T_r = 210$ kN $L_{max} = 4530$ mm $T_{1.0} = 473$ kN $T_{0.5} = 236$ kN

Double Angle Section Properties

 $r_x = 15.1 \text{ mm}$ $r_y = 26.0 \text{ mm}$ e = 12.8 mm

Double Angle Section Class

FLG= 3 Stem= 3 Overall = 3

Dongxiao Wu P. Eng.

T_r – Double angle factored tension resistance capacity considering eccentric moment, CSA S16-09 clause 13.9

 $T_{1.0}$ – 100% of (ϕ A_g F_y) CSA S16-09 clause 13.2 (a) (i)

T_{0.5} – 50% of (\$\phi\$ A_g F_y), this is normally the value used for connection design for connections without specified design force

L_{max} – Maximum allowed brace unsupported length, CSA S16-09 clause 10.4.2.2

2L64x64x6.4ELBB

Double Angle Tension Capacity

 $T_r = 165$ kN $L_{max} = 5850$ mm $T_{1.0} = 413$ kN $T_{0.5} = 207$ kN

Double Angle Section Properties

 $r_x = 19.5 \text{ mm}$ $r_y = 30.3 \text{ mm}$ e = 19.8 mm

Double Angle Section Class

FLG= 3 Stem= 3 Overall = 3

2L64x64x7.9ELBB

Double Angle Tension Capacity

 $T_r = 208$ kN $L_{max} = 5790$ mm $T_{1.0} = 510$ kN $T_{0.5} = 255$ kN

Double Angle Section Properties

 $r_x = 19.3 \text{ mm}$ $r_y = 30.7 \text{ mm}$ e = 19.2 mm

Double Angle Section Class

FLG= 3 Stem= 3 Overall = 3

2L64x64x9.5ELBB

Double Angle Tension Capacity

 $T_r = 250$ kN $L_{max} = 5730$ mm $T_{1.0} = 605$ kN $T_{0.5} = 302$ kN

Double Angle Section Properties

 $r_x = 19.1 \text{ mm}$ $r_y = 31.0 \text{ mm}$ e = 18.6 mm

Double Angle Section Class

FLG= 3 Stem= 3 Overall = 3

Dongxiao Wu P. Eng.

2.2.2.1.2 Unequal Angle Long Leg Back-to-Back

Tr - Double angle factored tension resistance capacity considering eccentric moment, CSA S16-09 clause 13.9

 $T_{1.0}$ - 100% of (ϕ A_g F_y) CSA S16-09 clause 13.2 (a) (i)

 $T_{0.5}-50\%$ of $(\phi A_g F_y)$, this is normally the value used for connection design for connections without specified design force

L_{max} – Maximum allowed brace unsupported length, CSA S16-09 clause 10.4.2.2

2L76x51x6.4LLBB

Double Angle Tension Capacity

 $T_r =$ **196** kN $L_{max} =$ **6840** mm $T_{1.0} =$ 413 kN $T_{0.5} =$ 207 kN

Double Angle Section Properties

 $r_x = 24.3 \text{ mm}$ $r_y = 22.8 \text{ mm}$ e = 18.8 mm

Double Angle Section Class

FLG= 3 Stem= 4 Overall = 4

2L76x51x9.5LLBB

Double Angle Tension Capacity

 $T_r = 306$ kN $L_{max} = 7050$ mm $T_{1.0} = 605$ kN $T_{0.5} = 302$ kN

Double Angle Section Properties

 $r_x = 23.9 \text{ mm}$ $r_y = 23.5 \text{ mm}$ e = 17.6 mm

Double Angle Section Class

FLG= 3 Stem= 3 Overall = 3

2L89x64x6.4LLBB

Double Angle Tension Capacity

 $T_r = 195$ kN $L_{max} = 8340$ mm $T_{1.0} = 500$ kN $T_{0.5} = 250$ kN

Double Angle Section Properties

 $r_x = 28.4 \text{ mm}$ $r_y = 27.8 \text{ mm}$ e = 22.7 mm

Double Angle Section Class

FLG= 3 Stem= 4 Overall = 4

2011-03-08 Rev 1.5 Page 198 of 211

Dongxiao Wu P. Eng.

T_r – Double angle factored tension resistance capacity considering eccentric moment, CSA S16-09 clause 13.9

 $T_{1.0}$ – 100% of (ϕ A_g F_y) CSA S16-09 clause 13.2 (a) (i)

T_{0.5} – 50% of (\$\phi\$ A_g F_y), this is normally the value used for connection design for connections without specified design force

L_{max} – Maximum allowed brace unsupported length, CSA S16-09 clause 10.4.2.2

2L89x64x9.5LLBB

Double Angle Tension Capacity

 $T_r = 360 \text{ kN}$ $L_{max} = 8400 \text{ mm}$ $T_{1.0} = 734 \text{ kN}$ $T_{0.5} = 367 \text{ kN}$

Double Angle Section Properties

 $r_x = 28.0 \text{ mm}$ $r_y = 28.4 \text{ mm}$ e = 21.5 mm

Double Angle Section Class

FLG= 3 Stem= 3 Overall = 3

2L102x76x6.4LLBB

Double Angle Tension Capacity

 $T_r = 165 \text{ kN}$ $L_{max} = 9810 \text{ mm}$ $T_{1.0} = 589 \text{ kN}$ $T_{0.5} = 294 \text{ kN}$

Double Angle Section Properties

 $r_x = 32.7 \text{ mm}$ $r_y = 32.8 \text{ mm}$ e = 32.4 mm

Double Angle Section Class

FLG= 4 Stem= 4 Overall = 4

2L102x76x7.9LLBB

Double Angle Tension Capacity

 $T_r = 275$ kN $L_{max} = 9720$ mm $T_{1.0} = 729$ kN $T_{0.5} = 365$ kN

Double Angle Section Properties

 $r_x = 32.4 \text{ mm}$ $r_y = 33.1 \text{ mm}$ e = 31.9 mm

Double Angle Section Class

FLG= 3 Stem= 4 Overall = 4

2011-03-08 Rev 1.5 Page 199 of 211

Dongxiao Wu P. Eng.

2.2.2.2 Horizontal Double Angle Brace

Design Basis & Assumption

- 1. Double angle <u>member capacity</u> under tension + eccentric moment governs the design. Brace <u>connection capacity</u>, including the effective net area caused by shear lag (CSA S16-09 clause 12.3.3.2), does not govern the design.
- 2. The eccentric moment is calculated using gusset plate thickness =10mm. The eccentricity value is shown in each chart.
- 3. Double angle maximum unsupported length is calculated as $L_{max} = min(rx, ry) \times 300$ as per CSA S16-09 clause 10.4.2.2
- 4. Double angle brace design yield strength = 300 MPa
- 5. Double angle flexural capacity is calculated based on AISC 360-05 section F9, tee stem in compression case.

2011-03-08 Rev 1.5 Page 203 of 211

Dongxiao Wu P. Eng.

2.2.2.2.1 Equal Angle Back-to-Back

Tr - Double angle factored tension resistance capacity considering eccentric moment, CSA S16-09 clause 13.9

 $T_{1.0}$ – 100% of (ϕ A_g F_y) CSA S16-09 clause 13.2 (a) (i)

 $T_{0.5}-50\%$ of $(\phi A_q F_v)$, this is normally the value used for connection design for connections without specified design force

Lmax - Maximum allowed brace unsupported length, CSA S16-09 clause 10.4.2.2

2L51x51x6.4ELBB

Double Angle Tension Capacity

 $T_r = 81$ kN $L_{max} = 4650$ mm $T_{1.0} = 327$ kN $T_{0.5} = 163$ kN

Double Angle Section Properties

 $r_x = 15.5$ mm $r_y = 21.6$ mm e = 20.0 mm

Double Angle Section Class

FLG= 3 Stem= 3 Overall = 3

2L51x51x9.5ELBB

Double Angle Tension Capacity

 $T_r = 111 \text{ kN}$ $L_{max} = 4530 \text{ mm}$ $T_{1.0} = 473 \text{ kN}$ $T_{0.5} = 236 \text{ kN}$

Double Angle Section Properties

 $r_x = 15.1 \text{ mm}$ $r_y = 22.1 \text{ mm}$ e = 21.2 mm

Double Angle Section Class

FLG= 3 Stem= 3 Overall = 3

Dongxiao Wu P. Eng.

T_r – Double angle factored tension resistance capacity considering eccentric moment, CSA S16-09 clause 13.9

 $T_{1.0}$ – 100% of (ϕ A_g F_y) CSA S16-09 clause 13.2 (a) (i)

 $T_{0.5}-50\%$ of $(\phi A_g F_y)$, this is normally the value used for connection design for connections without specified design force

L_{max} – Maximum allowed brace unsupported length, CSA S16-09 clause 10.4.2.2

2L64x64x6.4ELBB

Double Angle Tension Capacity

 $T_r = 110$ kN $L_{max} = 5850$ mm $T_{1.0} = 413$ kN $T_{0.5} = 207$ kN

Double Angle Section Properties

 $r_x = 19.5 \text{ mm}$ $r_y = 26.7 \text{ mm}$ e = 23.2 mm

Double Angle Section Class

FLG= 3 Stem= 3 Overall = 3

2L64x64x7.9ELBB

Double Angle Tension Capacity

 $T_r = 131$ kN $L_{max} = 5790$ mm $T_{1.0} = 510$ kN $T_{0.5} = 255$ kN

Double Angle Section Properties

 $r_x = 19.3 \text{ mm}$ $r_y = 27.0 \text{ mm}$ e = 23.8 mm

Double Angle Section Class

FLG= 3 Stem= 3 Overall = 3

2L64x64x9.5ELBB

Double Angle Tension Capacity

 $T_r = 150$ kN $L_{max} = 5730$ mm $T_{1.0} = 605$ kN $T_{0.5} = 302$ kN

Double Angle Section Properties

 $r_x = 19.1 \text{ mm}$ $r_y = 27.2 \text{ mm}$ e = 24.4 mm

Double Angle Section Class

FLG= 3 Stem= 3 Overall = 3

2011-03-08 Rev 1.5 Page 205 of 211